Panal Data 1: Framework

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Section 1

Introduction

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- Framework
- Cluster-Robust Standard Errors
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Introduction

- Panel data
  - n cross-sectional units at T time periods
  - Dataset (X_{it}, Y_{it})
- Examples:
  1. Person i's income in year t.
  2. Vote share in county i for the presidential election year t.
  3. Country i's GDP in year t.
- Panel data is useful
  1. More variation (both cross-sectional and temporal variation)
  2. Can deal with time-invariant unobserved factors.
  3. (Not focus in this course) Dynamics of individual over time.

Section 2

Framework

Framework

- Consider the model

$$y_{it} = \beta' x_{it} + \epsilon_{it}, E[\epsilon_{it}|x_{it}] = 0$$

  where x_{it} is a k-dimensional vector

- If there is no correlation between x_{it} and ϵ_{it}, you can estimate the model by OLS **(pooled OLS)**

- A natural concern here is the omitted variable bias.

- We now consider that ϵ_{it} is written as

$$\epsilon_{it} = \alpha_i + u_{it}$$

where α_i is called **unit fixed effect**, which is the time-invariant unobserved heterogeneity.

- With panel data, we can control for the unit fixed effects by incorporating the dummy variable for each unit i!

$$y_{it} = \beta' x_{it} + \gamma_2 D2_i + \cdots + \gamma_n Dn_i + u_{it}$$

where Dl_i takes 1 if $l = i$.
  - Notice that we cannot do this for the cross-section data!

- We write the model with unit FE as

$$y_{it} = \beta' x_{it} + \alpha_i + u_{it}$$

Framework

- The fixed effects model

$$y_{it} = \beta' x_{it} + \alpha_i + u_{it}$$

- Assumptions:
  1. u_{it} is uncorrelated with $(x_{i1}, \cdots, x_{iT})$, that is $E[u_{it}|x_{i1}, \cdots, x_{iT}] = 0$
  2. (Y_{it}, x_{it}) are independent across individual i.
  3. No outliers
  4. No Perfect multicollinearity

Assumption 1: Mean independence

- Assumption 1 is weaker than the assumption in OLS, because the time-invariant factor α_i is captured by the fixed effect.
  - Example: Unobserved ability is caputured by α_i.

Assumption 4: No Perfect Multicolinear.

- Consider the following regression with unit FE

$$wage_{it} = \beta_0 + \beta_1 experience_{it} + \beta_2 male_i + \beta_3 white_i + \alpha_i + u_{it}$$

  - $experience_{it}$ measures how many years worker i has worked before at time t.

- Multicollinearity issue because of $male_i$ and $white_i$.

- Intuitively, we cannot estimate the coefficient β_2 and β_3 because those **time-invariant** variables are completely captured by the unit fixed effect α_i.

Section 3

Estimation

Estimation (within transformation)

- Can estimate the model by adding dummy variables for each individual.
  - **least square dummy variables (LSDV) estimator**.
  - Computationally demanding with many cross-sectional units

- We often use the following **within transformation**.
- Define the new variable $\tilde{Y}_{it}$ as

$$\tilde{Y}_{it} = Y_{it} - \bar{Y}_i$$

  where $\bar{Y}_i = \frac{1}{T}\sum_{t=1}^{T} Y_{it}$.

- Applying the within transformation, can eliminate the unit FE α_i

$$\tilde{Y}_{it} = \beta' \tilde{X}_{it} + \tilde{u}_{it}$$

  - Then use the OLS estimator to the above equation!.

Importance of within variation in estimation

- The variation of the explanatory variable is key for precise estimation.
  - Remember the lecture "Regression 3"
- Within transformation eliminates the time-invariant unobserved factor,
  - a large source of endogeneity in many situations.
- But, within transformation also absorbs the variation of X_{it}.
- Remember that

$$\tilde{X}_{it} = X_{it} - \bar{X}_i$$

  - The transformed variable $\tilde{X}_{it}$ has the variation over time t within unit i.
  - If X_{it} is fixed over time within unit i, $\tilde{X}_{it} = 0$, so that no variation.

Other things to note

1. You can also add **time fixed effects (FE)**

$$y_{it} = \beta' x_{it} + \alpha_i + \gamma_t + u_{it}$$

   - The regression above controls for both **time-invariant individual heterogeneity** and **(unobserved) aggregate year shock**.
   - Panel data is useful to capture various unobserved shock by including fixed effects.

2. You can use IV regression with panel data.
   - The argument for the conditions of instruments should consider the presence of fixed effects.
   - Correlation (or uncorrelatedness) after controlling for the fixed effects.

Section 4

Inference

Cluster-Robust Standard Errors

- So far, we considered the two cases on the error structure
  1. Homoskedasticity $Var(u_i) = \sigma^2$
  2. Heteroskedasitcity $Var(u_i|x_i) = \sigma(x_i)$

- In the above case, we still assume the independence between observations, that is $Cov(u_i, u_{i'}) = 0$.

- In the panel data setting, we need to consider the **autocorrelation**.
  - the correlation between u_{it} and $u_{it'}$ across periods for each individual i.
- **Cluster-robust standard error** considers such autocorrelation.
  - The cluster is unit i. The errors within cluster are allowed to be correlated.
- For a more discussion, see Chapter 8 in "Mostly Harmless Econometrics".