	Parallel Trend	Research Strategy

Program Evaluation (Causal Inference) 2: Difference-in-differences

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Last updated: 2020-06-22

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Introduction

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Introduction

- Difference-in-differences (DID)
 - Exploit the panel data structure to estimate the causal effect.
- Consider that
 - Treatment and control group comparison: selection bias
 - Before v.s. After comparison: time trend
- ▶ DID combines those two comparisons to draw causal conclusion.

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DID in Figure (on screen)

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Plan of the Lecture

- Formal Framework
- Implementation in a regression framework
- Parallel Trend Assumption

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Reference				

- Angrist and Pischke "Mostly Harmless Econometrics" Chapter 5
- Marianne Bertrand, Esther Duflo, Sendhil Mullainathan, How Much Should We Trust Differences-In-Differences Estimates?, *The Quarterly Journal of Economics*, Volume 119, Issue 1, February 2004, Pages 249–275, https://doi.org/10.1162/003355304772839588
 - Discuss issues of calculating standard errors in the DID method.
- Hiro Ishise, Shuhei Kitamura, Masa Kudamatsu, Tetsuya Matsubayashi, and Takeshi Murooka (2019) "Empirical Research Design for Public Policy School Students: How to Conduct Policy Evaluations with Difference-in-differences Estimation" February 2019
 - Slide: https://slides.com/kudamatsu/did-manual/fullscreen/#
 - Paper: https://docs.google.com/viewer?a=v&pid=sites&srcid= ZGVmYXVsdGRvbWFpbnxta3VkYW1hdHN1fGd4OjM4YzkwYmVjM2ZmMz

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Framework

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Framework

- Consider two periods: t = 1, 2. Treatment implemented at t = 2.
- Y_{it}: observed outcome for person i in period t
- ► G_i: dummy for treatment group
- D_{it}: treatment status

 $D_{it} = 1 \text{ if } t = 2 \text{ and } G_i = 1$

- potential outcomes
 - Y_{it}(1): outcome for i when she is treated
 - $Y_{it}(0)$: outcome for *i* when she is not treated
- With this, we can write

$$Y_{it} = D_{it} Y_{it}(1) + (1 - D_{it}) Y_{it}(0)$$

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Identification

• Goal: ATT at t = 2

 $E[Y_{i2}(1) - Y_{i2}(0)|G_i = 1] = E[Y_{i2}(1)|G_i = 1] - E[Y_{i2}(0)|G_i = 1]$

What we observe

Pre-period $(t = 1)$	Post $(t = 2)$
$E[Y_{i1}(0) G_i = 1] \\ E[Y_{i1}(0) G_i = 0]$	$ \begin{split} E[Y_{i2}(1) G_i = 1] \\ E[Y_{i2}(0) G_i = 0] \end{split} $

Under what assumptions can we the ATT?

- Simple comparison if $E[Y_{i2}(0)|G_i = 1] = E[Y_{i2}(0)|G_i = 0]$.
- Before-after comparison if $E[Y_{i2}(0)|G_i = 1] = E[Y_{i1}(0)|G_i = 1]$.
- Other (more reasonable) assumption?

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Parallel Trend Assumption

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Assumption:

$$E[Y_{i2}(0) - Y_{i1}(0)|G_i = 0] = E[Y_{i2}(0) - Y_{i1}(0)|G_i = 1]$$

• Change in the outcome *without treatment* is the same across two groups.

Then,

$$\underbrace{E[Y_{i2}(1) - Y_{i2}(0)|G_i = 1]}_{ATT} = E[Y_{i2}(1)|G_i = 1] - E[Y_{i2}(0)|G_i = 1]$$
$$= E[Y_{i2}(1)|G_i = 1] - E[Y_{i1}(0)|G_i = 1]$$
$$- \underbrace{(E[Y_{i2}(0)|G_i = 1] - E[Y_{i1}(0)|G_i = 1])}_{= E[Y_{i2}(0) - Y_{i1}(0)|G_i = 0] \text{ (pararell trend)}}$$

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Thus,

$$ATT = E[Y_{i2}(1) - Y_{i1}(0)|G_i = 1] - E[Y_{i2}(0) - Y_{i1}(0)|G_i = 0]$$

which is why this is called "difference-in-differences".

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Estimation

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Estimation Approach

- 1. Plug-in estimator
- 2. Regression estimators

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Plug-in Estimator

Remember that the ATT is

 $ATT = E[Y_{i2}(1) - Y_{i1}(0)|G_i = 1] - E[Y_{i2}(0) - Y_{i1}(0)|G_i = 0]$

Replace them with the sample average.

$$AT\hat{T} = \{\bar{y}(t = 2, G = 1) - \bar{y}(t = 1, G = 1)\} \\ - \{\bar{y}(t = 2, G = 0) - \bar{y}(t = 1, G = 0)\}$$

where $\bar{y}(t, G)$ is the sample average for group G in period t.

Easy to make a 2 × 2 table!

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Example: Card and Kruger (1994)

	Stores by state			
Variable	PA (i)	NJ (ii)	Difference NJ – PA (iii)	
1. FTE employment before, all available observations	23.33	20.44	-2.89	
	(1.35)	(0.51)	(1.44)	
2. FTE employment after, all available observations	21.17	21.03	-0.14	
	(0.94)	(0.52)	(1.07)	
3. Change in mean FTE employment	-2.16	0.59	2.76	
	(1.25)	(0.54)	(1.36)	

Figure 1: image

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Regression Estimators

Run the following regression

$$y_{it} = \alpha_0 + \alpha_1 G_i + \alpha_2 T_t + \alpha_3 D_{it} + \beta X_{it} + \epsilon_{it}$$

- ► *G_i*: dummy for treatment group
- *T_t* :dummy for treatment period
- $D_{it} = G_i \times T_t$. α_3 captures the ATT.
- Regression framework can incorporate covariates X_{it}, which is important to control for observed confounding factors.

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Regression Estimators with FEs

With panel data

$$y_{it} = \alpha D_{it} + \beta X_{it} + \epsilon_i + \epsilon_t + \epsilon_{it}$$

where ϵ_i is individual FE and ϵ_t is time FE.

- Do not forget to use the cluster-robust standard errors!
 - See Bertrand, Duflo, and Mullainathan (2004, QJE) for the standard error issues.

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Parallel Trend

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Discussions on Parallel Trend

- Parallel trend assumption can be violated in various situations.
- Most critical issue: Treatment may depend on *time-varying factors* DID can only deal with **time-invariant factors**.
- Self-selection: participants in worker training programs experience a decrease in earnings before they enter the program
- Targeting: policies may be targeted at units that are currently performing best (or worst).

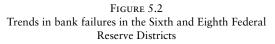
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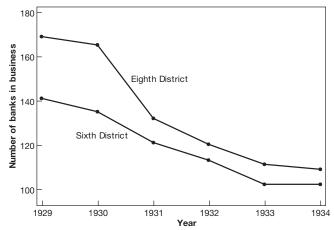
Diagnostics for Parallel Trends: Pre-treatment trends

- Check if the trends are parallel in the pre-treatment periods
- Requires data on multiple pre-treatment periods (the more the better)
- This is very popular. You MUST do this if you have multiple pre-treatment periods.
- Note: this is only diagnostics, NEVER a direct test of the assumption!
 You should never say "the key assumption for DID is satisfied if the pre-treatment trends are parallel.

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Example (Fig 5.2 from Mastering Metrics)





Note: This figure shows the number of banks in operation in Mississippi in the Sixth and Fighth Federal Reserve Districts between 1929 and 1934.

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Unit-Specific Time Trends

Add group-specific time trends as

$$y_{it} = \alpha D_{it} + \beta_1 G_i \times t + \epsilon_i + \epsilon_t + \epsilon_{it}$$

To see whether including the time trend does not change estimates that much. (robustness check)

Note that

- These time trends are meant to capture the trend in each group.
- At least 3 periods of the data is needed.
- But, these are assumed to be linear. We are not sure whether the trend is linear or not! So this is just a robustness check.

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Other Diagnostics: Placebo test

Placebo test using other period as treatment period.

$$y_{it} = \sum_{\tau} \gamma_{\tau} G_i \times I_{t,\tau} + \mu_i + \nu_t + \epsilon_{it}$$

- The estimates of γ_τ should be close to zero up to the beggining of treatment (Fig 5.2.4 of Angrist and Pischke)
- Placebo test using different dependent variable which should not be affected by the policy.

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Research Strategy

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Research Strategy using DID

Ishise et al (2019)

- $1. \ \mbox{How to find}$ a research question
- 2. What outcome dataset to look for
- 3. What policy to look for (except for example 1 and 2).